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PERFORMANCE AND GEOMETRY ANALYSIS OF ANTENNA ARRAY

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ABSTRACT

The radiation pattern of an antenna array depends strongly on the weighting method and the geometry of the array. Selection of the weights has received extensive attention, primarily because the radiation pattern is a linear function of the weights. However, the array geometry has received relatively little attention even though it also strongly influences the radiation pattern. The reason for this is primarily due to the complex way in which the geometry affects the radiation pattern. The main goal of this paper is to determine methods of optimizing array geometries in antenna arrays. An adaptive array with the goal of suppressing interference is investigated. It is shown that the interference rejection capabilities of the antenna array depend upon its geometry. Side-lobe level is an important metric used in antenna arrays, and depends on the weights and positions in the array. A method of determining optimal side-lobe minimizing weights is derived that holds for any linear array geometry, beam-width, antenna type and scan angle.

Keywords: Radiation pattern, Antenna arrays, Linear array geometry

INTRODUCTION

An antenna array is a set of N spatially separated antennas. Put simply, an array of antennas does a superior job of receiving signals when compared with a single antenna, leading to their widespread use in wireless applications. Arrays in practice can have as few as $N=2$ elements, which is common for the receiving arrays on cell phone towers. In general, array performance improves with added elements; therefore arrays in practice usually have more elements. Arrays can have several thousand elements, as in the AN/FPS-85 Phased

Array Radar Facility operated by U. S. Air Force. The array has the ability to filter the electromagnetic environment it is operating in based on the spatial variation of the signals present. There may be one signal of interest Or several, along with noise and interfering signals. The primary purpose of antenna systems is for communication; however, they are also used for detection. The information to be transmitted or received will be represented by $m(t)$. The message $m(t)$ will be assumed to be band-limited to B Hz, meaning almost all the energy has frequency content below B Hz. In the earlier days of radio, $m(t)$ had the information coded directly into the amplitude or frequency of the signal (as in AM or FM radio). Information today is primarily encoded into digital form, and $m(t)$ is a train of a discrete set of symbols

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representing 1s and 0s. The information is still encoded into the amplitude and phase of these symbols; however, the amplitudes and phases now take on a discrete set of values.

REVIEW

The first articles on improving array performance via geometry optimization dates back to the early 1960s. Unz studied linear arrays in 1960 and noted that performance improvement could be obtained by holding the weights constant and varying the element positions. In 1960, King proposed eliminating grating lobes via element placement in an array. In 1961, Harrington considered small element perturbations in an attempt to synthesize a desired array pattern.

The concept of ‘thinned arrays’ was introduced in the early 1960s as well. It was noted that in large, periodically spaced antenna arrays, removing some of the elements did not noticeably degrade the array’s performance. This method of altering an array’s geometry was introduced by Skolnik *et al.* and was first studied deterministically – attempting to systematically determine the minimum number of elements required to achieve a desired performance metric. For large arrays, the problem was tackled in a statistical fashion to avoid the excessive amount of computation time required to determine an optimal thinned array.

Stutzman introduced a simple method of designing non uniformly spaced linear arrays that is based on Gaussian-quadrature that involves fairly simple calculations. In addition, he showed that by appropriate scaling of the element spacings, some of the elements will lie in the region where the ideal source has a small excitation, and thus can be omitted from the array (another method of array thinning).

Array geometry plays a critical roll in the direction-finding capabilities of antenna

arrays. Pillai *et al.* shows that for linear aperiodic arrays, there exists an array that has superior spatial-spectrum estimation ability. Gavish and Weiss compared array geometries based on how distinct the steering vectors are for distinct signal directions; they proposed that larger distinctions lead to less ambiguity in direction finding. Ang *et al.* also evaluated the direction-finding performance of arrays by varying the elements’ positions based on a genetic algorithm.

Antenna arrays are also used for diversity reception, or comparing signal power at spatially distinct locations and processing the signals based on their relative strength. A textbook proof analyzing uniformly distributed multipath components suggest arrays will exhibit good diversity characteristics if the antennas are separated by at least 0.4λ . An analytical method of choosing a linear array geometry for a given set of weights is presented in; this method was also extended to circular and spherical arrays. This method requires a specified array pattern and set of weights; it then attempts to determine an array geometry that closely approximates the desired array pattern. The method does not guarantee a global optimum for the element positions. In the weights are optimized and then linear array scaled to find an optimal geometry. A method of perturbing element positions to place nulls in desired directions is described. Due to the large increase in the computational capability of computers, array geometry optimization has been under investigation recently using biologically inspired algorithms, such as Genetic Algorithms (GA). Khodier and Christodoulou used the Particle Swarm Optimization (PSO) method to determine optimal side-lobe-minimizing positions for linear arrays assuming the weights were constant. In, PSO methods were used for

planar array synthesis in minimizing side-lobes, along with null-placement. Tennant *et al.* used a genetic algorithm to reduce side-lobes via element position perturbations. The authors demonstrate side-lobe minimization by choosing geometry based on the Ant Colony Optimization (ACO) method.

In addition to geometry considerations, the minimum possible side-lobe level for an array is of interest. For linear, equally spaced arrays, the problem of determining the optimal weights was solved by Dolph and published in 1946. This method is known as the Dolph-Chebyshev method, because Dolph uses Chebyshev polynomials to obtain the excitation coefficients. The method returns the minimum possible null-to-null beam-width for a specified side-lobe level (or equivalently, the minimum possible side-lobe level for a specified null-to-null beam-width). This method has an implicit maximum array spacing for a given beam-width. Riblet showed that for arrays with inter-element spacing less than $\lambda / 2$, there exists a set of weights that give a smaller null-to-null main beam than Dolph's method. However, Riblet only derives the results for arrays with an odd number of elements. The Dolph-Chebyshev method produces side-lobes that have equal amplitudes. A more generalized version of Dolph's algorithm (called an equi-ripple filter) is also frequently used in the design of Finite Impulse Response (FIR) filters in the field of signal processing.

In 1953, DuHamel extended the work of Dolph to end fire linear arrays with an odd number of elements. Dolph's work was also considered for the case of non-isotropic sensors; the problem was not solved for the general case. The optimum side-lobe minimizing weights for broadside, non-uniformly spaced symmetric linear arrays with real weights can now be found using

linear programming. The authors attempt to simultaneously optimize the weights and the positions of a 25-element linear array using a Simulated Annealing (SA) algorithm. They make no claim that their results are optimal, but do show the side-lobes lowered via the optimization method. Adaptive antenna arrays began with the work of Bernard Widrow in the 1960s. Optimizing an adaptive antenna array's geometry was performed in with regards to suppressing interference; this work is the subject of Linear Arrays.

PROBLEM STATEMENT AND SOLUTION

In constructing linear and planar arrays the radiation properties of distinct patterns must be analyzed in order to optimize the array for certain uses. The first example of antenna arrays we looked at were linear arrays upon which we placed "n" number of elements. We used MATLAB to calculate the constructive and destructive interference in terms of the array factor (AF), that characterizes the radiated field. Here, N is the number of elements in the X-axis, IN is the charge per element, d/λ is the ratio of the distance between each element in wavelengths, and alpha is a phase shift which changes the direction of the main beam. To simplify calculations, we kept the charge equal for all elements. We also chose to keep alpha equal to zero due to the effects that phase has on the main beam. MATLAB used a "while" loop function to calculate the sum of the array factors for n elements a distance dB apart with uniform voltage. As the elements were placed within 1 wavelength, there was constructive interference such that there was always one main lobe with smaller side lobes as more elements were added. The main lobe with high side lobes, which were normalized by taking the $20 \cdot \log_{10}$ of the array factor. This

scaling allowed for better analysis of the side lobes and their characteristics.

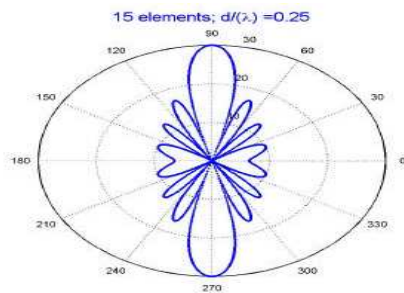


Fig. 1: Main lobe with high side beams. 15 elements were placed an equal distance dB apart.

SIMULATION AND RESULT

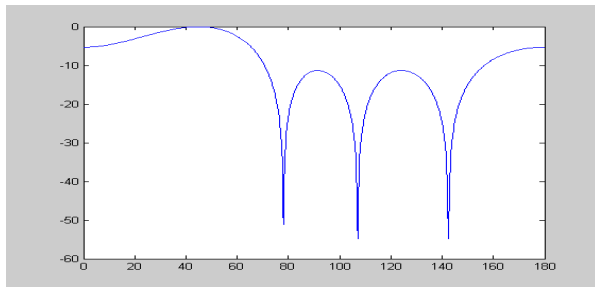
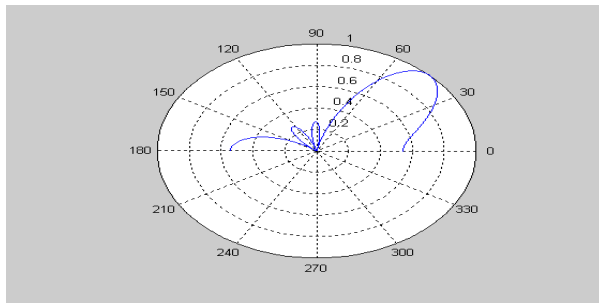


Fig. 2: Linear steering array

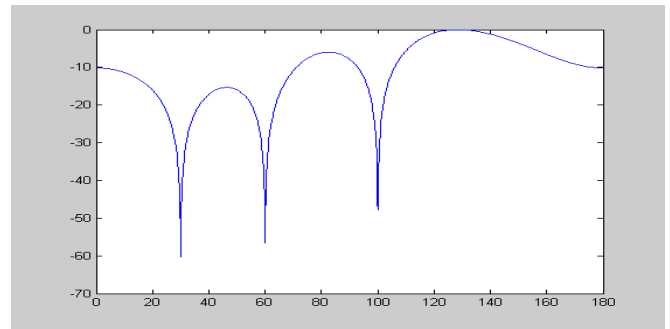
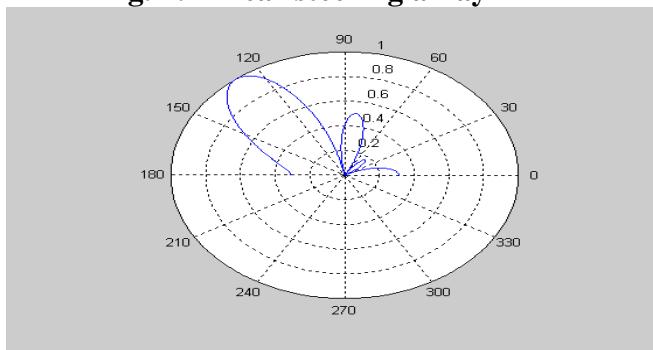


Fig. 3: Calculation of Directivity

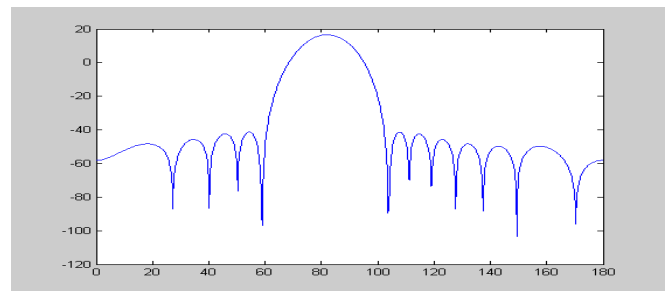
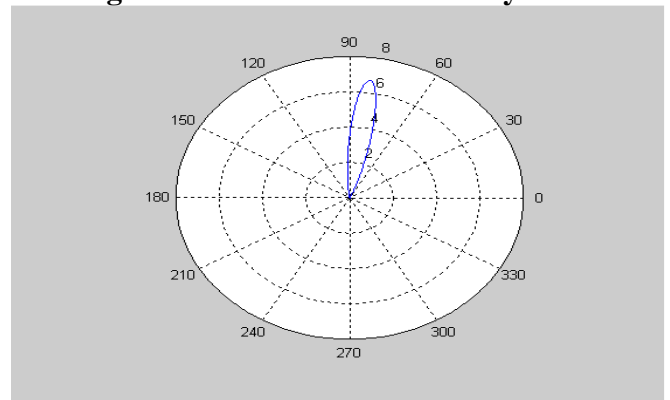


Fig. 4: Linear DBF transmitter

DISCUSSION

As the field of signal processing developed, arrays could be used to receive energy (or information) from a particular direction while rejecting information or nulling out the energy in unwanted directions. Consequently, arrays could be used to mitigate intentional interference (jamming) or unintentional interference (radiation from other sources not meant for the system in question) directed toward the communication system. Further development in signal processing led to the concept of adaptive antenna arrays. These

arrays adapted their radiation or reception pattern based on the environment they were operating in. This again significantly contributed to the capacity available in wireless communication systems.

CONCLUSION

The goal of this paper has been to show the effect of an array's geometry on metrics of interest. These metrics include side-lobe level, interference rejection. Because of the difficulty in analyzing an array's geometry, the geometry is often chosen to be a standard geometry in practice. However, this work has shown that gain in performance can be achieved via suitable optimization of the array geometry.

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